

Math 111 – Spring 2014
Examination 1

Please complete the following problems. All work must be shown in order to receive full credit. Answers without explanation will receive *no* credit. The use of books, notes, calculators, or any other external sources of information is not allowed during this examination.

1.(10 pts.) Evaluate the following limits, allowing $+\infty$ and $-\infty$ as possible values of a limit. If the limit does not exist, explain why.

a. $\lim_{x \rightarrow 3} \frac{2x - 6}{x^2 - 2x - 3}$

b. $\lim_{x \rightarrow 0} \frac{\tan(3x)}{\sin(2x)}$

2.(10 pts.) Evaluate the following limits, allowing $+\infty$ and $-\infty$ as possible values of a limit. If the limit does not exist, explain why.

a. $\lim_{x \rightarrow 1} \frac{\sqrt{x}}{\sqrt{x+1} - \sqrt{x-1}}$

b. $\lim_{x \rightarrow 0^+} e^{-\frac{1}{x}}$

3.(10 pts.) Evaluate the following limits, allowing $+\infty$ and $-\infty$ as possible values of a limit. If the limit does not exist, explain why.

a. $\lim_{x \rightarrow 2} \frac{x - 2}{2 - \sqrt{x + 2}}$

b. $\lim_{x \rightarrow \infty} \arcsin\left(\frac{x^2 + 7}{2x^2 + 9x + 3}\right)$

4.(10 pts.) Evaluate the following limits, allowing $+\infty$ and $-\infty$ as possible values of a limit. If the limit does not exist, explain why.

a. $\lim_{x \rightarrow 4^-} \frac{3}{\sqrt{x} - 2}$

b. $\lim_{x \rightarrow 0^+} \left(\frac{1}{x} - \frac{1}{x^2 + x}\right)$

5.(12 pts.) Find the slope of the tangent line as the limit of a difference quotient for $f(x) = \frac{1}{\sqrt{x}}$ at $x = 1$.

6.(20 pts.) Find all horizontal, vertical, and slant (oblique) asymptotes, if they exist, for the following functions. Be sure to clearly label the type of each of your asymptotes.

a. $y = \frac{2x^2 + 1}{2x + 2}$

b. $y = \frac{x^2 + 2x}{x^3 - x^2 + x - 1}$

7.(14 pts.) Find all points where f is discontinuous and identify the type of discontinuity.

$$f(x) = \frac{|2 - x|}{2x - x^2}$$

8.(14 pts.) Find all values of α and β , if any, which make f continuous for all x .

$$f(x) = \begin{cases} \alpha x + \beta & x \leq -1 \\ \arctan(x) & -1 < x < 1 \\ \alpha x + \beta & x \geq 1 \end{cases}$$