3.2 - Polynomial Functions

Review problems

1. Solving polynomial equations. Solve the following:

(a) $x^4 = 81x^2$ (b) $(x-2)^2(x+4)(x-10)^3 = 0$

2. Finding intercepts. Find x- and y-intercepts of:

(a)
$$y = x^2 + 3x$$
 (b) $y = 2(x - 3)^2$

Basic knowledge

- 3. Find zeros, the multiplicity of each zero, end-behavior, and y-intercept, and then sketch the graph of each polynomial function:
 - (a) $f(x) = 2x(x-3)^2(x+4)^7$ (b) $f(x) = -3(x-1)(x+2)^2$

Intermediate

4. Find zeros, the multiplicity of each zero, end-behavior, and y-intercept, and then sketch the graph of the given polynomial function:

 $f(x) = x - x^3$

Advanced

5. Find all real zeros, the multiplicity of each real zero, end-behavior, and y-intercept, and then sketch the graph of the given polynomial function:

 $f(x) = x(x^2 + 1)$

6. Write an equation of a polynomial function of degree 4 that has a zero -1 of multiplicity 2, a zero 4 of multiplicity 1, and a zero 2 of multiplicity 1 and the y-intercept at (0, -12).