2.4 - Relations and Functions and 2.5 - Properties of Functions

Review problems

1. **Solving linear inequalities.** Solve the given inequalities. Write answers in interval notation.

(a)
$$2x - 5 > 3$$

(b)
$$5 - 4x \le 2x + 7$$

2. **Solving equations.** Solve for *y* in terms of *x*:

(a)
$$2y - 5x = 3$$

(b)
$$v^2 - 4 = x$$

Basic knowledge

3. Do the following equations define y as a function of x?

(a)
$$7x^2 + 5y = 9$$
 (b) $y^4 - x = 0$ (c) $x - 4 = 0$ (d) $y = 2$

(b)
$$y^4 - x = 0$$

(c)
$$x - 4 = 0$$

(d)
$$y = 2$$

4. Let
$$f(x) = \frac{3+x}{x-4}$$
:

- (a) find the function's domain
- (b) evaluate f(3), f(-2)
- (c) find intercepts
- (d) find and simplify f(-x), f(x + 5), f(a + h)
- 5. Detrmine algebraically whether the given functions are odd, even, or neither.

(a)
$$f(x) = 5x - 2$$

(b)
$$g(x) = -x + x^3$$

(b)
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 (c) $h(x) = -x^2 - 9$

Intermediate
6. Let
$$f(x) = \frac{\sqrt{2x-6}}{x-5}$$
:

- (a) find the function's domain
- (b) evaluate f(3), f(-2)
- (c) find intercepts
- (d) find and simplify f(-x), f(x+5), f(a+h)

Advanced

- 7. Find the domain of function $g(x) = \sqrt{\frac{\sqrt{3x-8}}{3x-8}}$
- 8. For function $f(x) = x^2 2x + 3$ find and simplify:

(a)
$$f(x + h)$$

(a)
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 (b) $\frac{f(x + h) - f(x)}{h}$