

MATH 656: Complex Variables I

Spring 2022 Course Syllabus

NJIT Academic Integrity Code: All Students should be aware that the Department of Mathematical Sciences takes the University Code on Academic Integrity at NJIT very seriously and enforces it strictly. This means that there must not be any forms of plagiarism, i.e., copying of homework, class projects, or lab assignments, or any form of cheating in quizzes and exams. Under the University Code on Academic Integrity, students are obligated to report any such activities to the Instructor.

Please be sure you read and fully understand our [DMS Online Exam Policy](#).

COURSE INFORMATION

Course Description: The theory and applications of analytic functions of one complex variable: elementary properties of complex numbers, analytic functions, elementary complex functions, conformal mapping, Cauchy integral formula, maximum modulus principle, Laurent series, classification of isolated singularities, residue theorem, and applications.

Number of Credits: 3

Prerequisites: [MATH 545](#) or [MATH 645](#) or departmental approval.

Course-Section and Instructors:

Course-Section	Instructor
Math 656-002	Professor L. Cummings

Office Hours for All Math Instructors: [Spring 2022 Office Hours and Emails](#)

Textbook: Full notes for the course will be provided. A suggested supplementary reference text is:

Title	<i>Complex Variables: Introduction & Applications</i>
Author	M.J. Ablowitz and A.S. Fokas
Edition	2nd
Publisher	2nd Ed
ISBN #	ISBN-13: 978-0521534291; ISBN-10: 0521534291

University-wide Withdrawal Date: The last day to withdraw with a W is **Monday, April 4, 2022**. It will be strictly enforced.

COURSE GOALS

Course Objectives:

- Student gain a clear and intuitive understanding of the wide-ranging properties of analytic functions of a complex variable.
- Students learn and understand key theorems applicable to analytic functions, particularly the Integral Theorems, their corollaries and applications.
- Students learn key applications of the Cauchy Residue Theorem, including its use in Fourier and Laplace Transform theory.
- Students gain practical knowledge of how complex analysis can be used in a range of applied mathematics and physics problems.

Course Outcomes:

- Students will be able to use and apply results from complex analysis to a range of problems in applied mathematics.
- Students will be prepared for the complex analysis portion of Part B of the written Qualifying Exam.
- Students will gain an understanding of the theory of functions of a complex variable.
- Students will be prepared for the next level of study in complex analysis and other areas of mathematics.

Course Assessment:

The assessment of objectives will be achieved through homework assignments and examinations testing the specific outcomes listed above.

POLICIES

DMS Course Policies: All DMS students must familiarize themselves with, and adhere to, the [Department of Mathematical Sciences Course Policies](#), in addition to official [university-wide policies](#). DMS takes these policies very seriously and enforces them strictly.

Grading Policy: The final grade in this course will be determined as follows:

Homework	20%
Midterm Exam	30%
Final Exam	50%

Your final letter grade will be based on the following tentative curve.

A	88 - 100	C	62 - 67
B+	82 - 87	D	55 - 61
B	75 - 81	F	0 - 54
C+	68 - 74		

Attendance: Attendance in class is mandatory. A couple missed lectures over the course of the semester will not impact your grade, but please don't miss class if you don't have to.

Email and Canvas: Regularly check your NJIT email account and the course information posted on Canvas for class assignments and announcements from your instructor.

Homework: Homework problem sets will be assigned regularly by the instructor via canvas and will include problems requiring basic coding in MATLAB or Mathematica. Due dates as posted on canvas; late work is not accepted (rare exceptions may be made if there is good reason). All HW assignments are to be submitted via the canvas course page (NOT email).

Exams: The midterm exam will be held at the regular class time as indicated in the detailed schedule below, proctored by the instructor.

Midterm Exam	March 11, 2022
Final Exam Period	May 6 - May 12, 2022

The final exam will test your knowledge of all the course material taught in the entire course. Make sure you read and fully understand the **Math Department's Examination Policy**. This policy will be strictly enforced.

Makeup Exam Policy: There will be **NO MAKE-UP QUIZZES OR EXAMS** during the semester. In the event an exam is not taken under rare circumstances where the student has a legitimate reason for missing the exam, the student should contact the Dean of Students office and present written verifiable proof of the reason for missing the exam, e.g., a doctor's note, police report, court notice, etc. clearly stating the date AND time of the mitigating problem. The student must also notify the Math Department Office/Instructor that the exam will be missed.

Cellular Phones: All cellular phones and other electronic devices must be switched off during all class times.

ADDITIONAL RESOURCES

Further Assistance: For further questions, students should contact their instructor. All instructors have regular office hours during the week. These office hours are listed on the Math Department's webpage for **Instructor Office Hours and Emails**.

Accommodation of Disabilities: The Office of Accessibility Resources and Services (OARS) offers long term and temporary accommodations for undergraduate, graduate and visiting students at NJIT.

If you are in need of accommodations due to a disability please contact Scott Janz, Associate Director of Disability Support Services at **973-596-5417** or via email at **scott.p.janz@njit.edu**. The office is located in Kupfrian Hall, Room 201. A Letter of Accommodation Eligibility from the Office of Accessibility Resources and Services office authorizing your accommodations will be required.

For further information regarding self identification, the submission of medical documentation and additional support services provided please visit the Office of Accessibility Resources and Services (OARS) website at:

<https://www.njit.edu/studentsuccess/accessibility/>

Important Dates (See: **Spring 2022 Academic Calendar, Registrar**)

Date	Day	Event
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January 18, 2022	Tuesday	First Day of Classes
January 22, 2022	Saturday	Saturday Classes Begin
January 24, 2022	Monday	Last Day to Add/Drop Classes
March 14, 2022	Monday	Spring Recess Begins
March 19, 2022	Saturday	Spring Recess Ends
April 4, 2022	Monday	Last Day to Withdraw
April 15, 2022	Friday	Good Friday - No Classes
April 17, 2022	Sunday	Easter Sunday - No Classes
May 3, 2022	Tuesday	Friday Classes Meet
May 3, 2022	Tuesday	Last Day of Classes
May 4 - May 5, 2022	Wednesday and Thursday	Reading Days
May 6 - May 12, 2022	Friday to Thursday	Final Exam Period

Course Outline

Lecture (date)	Sections	Topic
1 (1-18)	1	Introduction: Complex numbers and their properties
2 (1-21)	1, 2	Simple complex equations; sets in the complex plane
3 (1-25)	2, 3	Paths in the complex plane; introduction to analytic functions
4 (1-28)	3	Complex sequences, series & functions
5 (2-1)	3	Differentiability & analyticity
6 (2-4)	3	Multivalued functions & branch cuts
7 (2-8)	3	Complex integration: introduction
8 (2-11)	4	Complex integration
9 (2-15)	5	Cauchy's theorem
10 (2-18)	5	Cauchy's theorem and related results
11 (2-22)	5	Further Cauchy theorems and Maximum Modulus
12 (2-25)	6	Morera and Liouville theorems
13 (3-1)	7	Taylor's theorem
14 (3-4)	7	Identity theorem
15 (3-8)	7	Review
16 (3-11)	Exam	
Spring	Break	
17 (3-22)	7	Open Mapping theorem
18 (3-25)	8	Laurent expansions
19 (3-29)	8,9	Laurent expansions & Cauchy's Residue Theorem
20 (4-1)	9	Residue theorem and applications
4th April	Last Day to Withdraw	
21 (4-5)	9	More applications of residue theory
22 (4-8)	10	Fourier Transform

23 (4-12)	10	Fourier and Laplace Transform
15th April		Good Friday
24 (4-19)	10	Laplace Transform
25 (4-22)	11	Conformal mappings
26 (4-26)	11	Conformal mappings
27 (4-29)	11	Conformal mappings
28 (5-3)	Last Class: Final Exam Review	

*Updated by Professor I. Cummings - 1/13/2022
Department of Mathematical Sciences Course Syllabus, Spring 2022*